

2.1 Worksheet

Algebra 2

Name: _____

For #1 – 10 use the matrices: $A = \begin{bmatrix} 5 & 0 \\ -1 & 2 \end{bmatrix}$, $B = \begin{bmatrix} -3 & 8 \\ -5 & 10 \end{bmatrix}$, $C = \begin{bmatrix} 3.2 & 1 \\ -1.5 & 0 \end{bmatrix}$.

1. $A + B$

2. $A - B$

3. $C + A$

4. $B - C$

5. $2A$

6. $5A$

7. $-C$

8. $-3A + B$

9. $A + B + 2C$

10. $-10C + A$

11. $B + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$

For #12-13, find the missing values:

12. $\begin{bmatrix} 5 & z + 3 \\ -1 & 2 \\ 9 + x & y \end{bmatrix} = \begin{bmatrix} a + 3 & -50 \\ b - 8 & 2 + c \\ 15 & 2.5 \end{bmatrix}$

13. $3 \begin{bmatrix} 5 & x + 1 & 6 \\ y - 3 & z & 2 \end{bmatrix} = \begin{bmatrix} 15 & 24 & 18 \\ 21 & 0 & 6 \end{bmatrix}$

For #14-16, find the missing values:

$$14. \begin{bmatrix} 8 & z-1 \\ b+2 & 3+c \\ 10-x & y+1 \end{bmatrix} = \begin{bmatrix} a-1 & -5 \\ -8 & 2 \\ 8 & 5.5 \end{bmatrix}$$

$$15. 2 \begin{bmatrix} 7.5 & 2x-2 & 6 \\ y+7 & 4z & 5 \end{bmatrix} = \begin{bmatrix} 15 & 20 & 12 \\ 2 & 20 & 10 \end{bmatrix}$$

$$16. [3 \ 2 \ x] - 2[y \ z - 5 \ 10] = [-1 \ 14 \ -8]$$

17. In the price matrix P , the rows represent prices for sweatshirts and sweatpants. The columns represent the color scheme of the items: white, red, and tie-dye. If the sales tax rate is 7%, find the sales tax of each item.

$$P = \begin{bmatrix} 30 & 40 & 50 \\ 25 & 35 & 55 \end{bmatrix}.$$

For #1 – 7 use the matrices to find the dot product, or if it is not possible to multiply them, tell why.

$$A = \begin{bmatrix} 8 & 7 & -4 \\ 1 & -4 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} -9 & -7 \\ -2 & 2 \\ 10 & 9 \end{bmatrix}, \quad C = \begin{bmatrix} -1 & -5 \\ -2 & 8 \end{bmatrix}, \quad D = \begin{bmatrix} -10 \\ 1 \\ 7 \end{bmatrix}, \quad E = [10 \quad -5 \quad -5]$$

1. $A \cdot B$ 2. $B \cdot A$ 3. $A \cdot C$ 4. $B \cdot C$ 5. $C \cdot D$ 6. $D \cdot E$ 7. $E \cdot D$

8. Find IQ , if $I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ and $Q = \begin{bmatrix} 1 & -3 & 2 \\ -4 & 5 & -6 \\ 9 & -7 & 8 \end{bmatrix}$

11. Raul owns and operates two souvenir stands. At his baseball park stand, sweatshirts cost \$45 and T-shirts cost \$20. At his football stadium stand, sweatshirts cost \$50 and T-shirts cost \$15. Today Raul sold 20 sweatshirts and 25 T-shirts at each stand. Use matrix multiplication to find the total amount in daily sales at each souvenir stand.

For #12-13: A drama teacher assigns final grads in her class based on the weighted system shown below.

The matrix G represents the grades for Kiyo and his two friends, Rachel and Leo. $G = \begin{matrix} & \begin{matrix} tests \\ proj \\ part \end{matrix} & \begin{bmatrix} 90 & 83 & 78 \\ 94 & 88 & 96 \\ 98 & 94 & 89 \end{bmatrix} \end{matrix}$

12. Write matrix W as a 1×3 matrix to represent the weighted grading system.

Drama Syllabus
Tests 45%
Projects 30%
Participation 25%

13. Perform matrix multiplication to find the final grades for each of the three students.

For 1 – 5, find the determinants of the following matrices, or if it's not possible, explain why:

1. $\begin{bmatrix} -8 & -9 \\ 5 & -10 \end{bmatrix}$

2. $\begin{bmatrix} -2 & -4 \\ 10 & -10 \end{bmatrix}$

3. $\begin{bmatrix} 7 & 2 & -6 \\ 10 & 5 & -4 \end{bmatrix}$

4. $\begin{bmatrix} -5 & 9 & 9 \\ -10 & -8 & 4 \\ 10 & 3 & -4 \end{bmatrix}$

5. $\begin{bmatrix} -9 & 10 & -6 \\ -2 & -8 & -5 \\ 7 & -3 & 2 \end{bmatrix}$

For #6-10, Does each given matrix have an inverse? If so, find it.

$$6. P = \begin{bmatrix} 1 & -3 \\ -1 & 4 \end{bmatrix}$$

$$7. R = \begin{bmatrix} -2 & 8 & -5 \\ 3 & -11 & 7 \\ 9 & -34 & 21 \end{bmatrix}$$

$$8. Q = \begin{bmatrix} -6 & -9 \\ -4 & -6 \end{bmatrix}$$

$$9. S = \begin{bmatrix} -24 & 18 & 5 \\ 20 & -15 & -4 \\ -5 & 4 & 1 \end{bmatrix}$$

$$10. \text{ Are } \begin{bmatrix} 8 & 4 \\ 4 & -2 \end{bmatrix} \text{ and } \begin{bmatrix} \frac{1}{16} & \frac{1}{8} \\ \frac{1}{8} & -\frac{1}{4} \end{bmatrix} \text{ inverses? Explain how you know.}$$

For #1-2, Solve the matrix $A \cdot X = B$ for the following matrices:

1. $A = \begin{bmatrix} 8 & -7 \\ -6 & 4 \end{bmatrix}$, $B = \begin{bmatrix} 11 \\ -12 \end{bmatrix}$

2. $A = \begin{bmatrix} 2 & 8 & 4 \\ 1 & -1 & -3 \\ -3 & 2 & -9 \end{bmatrix}$, $B = \begin{bmatrix} 26 \\ -2 \\ 37 \end{bmatrix}$

For #3-6, Rewrite each system as a Matrix equation, then solve using inverse matrices, if possible.

3.
$$\begin{cases} -x + 2y = 8 \\ -3x + 6y = -12 \end{cases}$$

4.
$$\begin{cases} x + 2y + 3z = -8 \\ 3x - 2y + z = -1 \\ x + y - 2z = 6 \end{cases}$$

5.
$$\begin{cases} -3x + 4y = -4 \\ \frac{1}{2}x - 3y = -11 \end{cases}$$

6.
$$\begin{cases} 2x + \frac{2}{3}y + z = -8 \\ x + 2y - \frac{1}{3}z = 6 \\ -\frac{1}{2}x + 3y - 2z = 22 \end{cases}$$

For #7-8: Luke had some quarters and dimes in his pocket. The quarters and dimes are worth \$2.55. He has 3 times as many quarters as dimes.

7. Write a matrix equation to find the number of quarters, x , and dimes, y , Luke has.

8. How many quarters and dimes does Luke have?

9. The coordinates (x, y) of a point in a plane are the solution of the matrix equation $\begin{bmatrix} -1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -5 \\ 2 \end{bmatrix}$. In what quadrant is the point located?