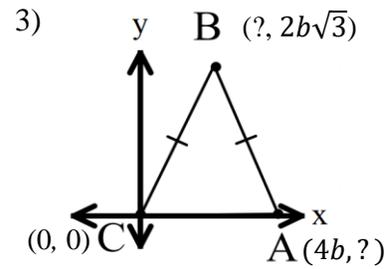
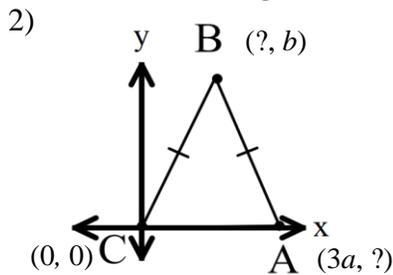
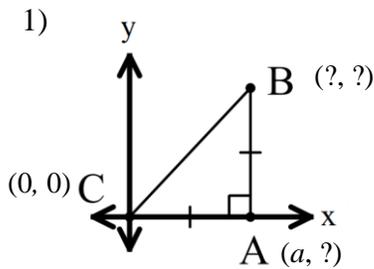


Formal Geometry

Do all work on your own paper!

For #1 – 3, find the missing coordinates for each triangle.



For #4 – 6, classify each triangle as scalene, isosceles, or equilateral. Provide evidence for your decision.

4) $X(-5, 9); Y(2, 1); Z(-8, 3)$

5) $A(7, 6); Y(5, 1); Z(9, 1)$

6) $P(3, -2); Q(1, -4); R(3, -4)$

For #7 – 8: Given $\triangle XYZ$ with $X(0, 0); Y(2h, 2h); Z(4h, 0)$.

7) Find the slope of each side of the triangle. Is the triangle a right triangle? Explain your reasoning.

8) Classify the triangle as scalene, isosceles, or equilateral. Provide evidence for your decision.

For #9 – 10: Given $\triangle ABC$ with $A(0, 0); B(a, b); C(2a, 0)$.

9) Find the slope of each side of the triangle. Is the triangle a right triangle? Explain your reasoning.

10) Classify the triangle as scalene, isosceles, or equilateral. Provide evidence for your decision.

11) A right triangle has vertices at $(0, 0)$ and $(a, 0)$. Which options below could be the coordinates of the third vertex? Choose all that apply.

A) $(0, a)$

B) $(-a, 0)$

C) (a, a)

D) $((0, -a)$

F) $(a, -a)$

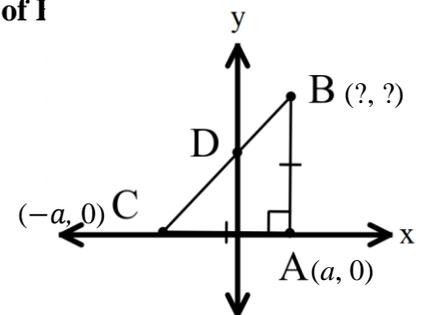
G) $(-a, -a)$

For #12 – 14: $\triangle ACB$ is an isosceles right triangle. Point D is the midpoint of \overline{AB} .

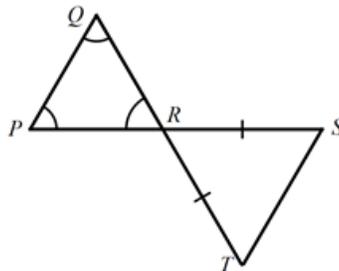
12) Find the coordinates of point B .

13) Find the coordinates of point D .

14) Find the slopes of AC and AB . Explain how these slopes support that $\triangle ACB$ is a right triangle.



15) Find the measure of $\angle S$.



Answers:

1) $A(a, 0); B(a, a)$

2) $A(3a, 0); B(1.5a, b)$

3) $A(4b, 0); B(2b, 2b\sqrt{3})$

4) Scalene

5) Isosceles

6) Isosceles

7) slope of $XY = 1$; slope of $YZ = -1$; slope of $XZ = 0$. Thus, the triangle is a right triangle, because two sides have slopes that are opposite reciprocals, and so $XY \perp YZ$, forming a right angle.

8) The triangle is isosceles, because $XY = 2h\sqrt{2}$; $YZ = 2h\sqrt{2}$ and $XZ = 4h$.

9) slope of $AB = \frac{b}{a}$; slope of $BC = -\frac{b}{a}$; slope of $AC = 0$. Thus, the triangle is a not right triangle, because none of the sides have slopes that are opposite reciprocals, and so no sides are perpendicular.

10) The triangle is isosceles, because $AB = \sqrt{a^2 + b^2}$, $BC = \sqrt{a^2 + b^2}$, and $AC = 2a$.

11) A, C, D, and F

12) $(a, 2a)$

13) $(0, a)$

14) slope of $AC = 0$; slope of $AB = \text{undefined}$. All horizontal lines have a slope of 0; all vertical lines have a slope of undefined. Any vertical line is perpendicular to any horizontal line if the lines are coplanar, and so the triangle has a right angle.

15) 60°

4.7 Worksheet