

Prob/Stat/Discrete

Homework 1.4

Name _____

In exercises 1-3, find each of the following sets using,

$$U = \{1, 2, 3, 4, 5, 6, 7\}$$

$$A = \{1, 3, 5, 7\}$$

$$B = \{1, 2, 3\}$$

$$C = \{2, 3, 4, 5, 6\}$$

1. $A \cap (B \cup C)$
2. $(C' \cap A) \cup (C' \cap B')$
3. $(B \cup C)' \cap A$

In Exercises 4-6, find each of the following sets using,

$$U = \{a, b, c, d, e, f, g, h\}$$

$$A = \{a, g, h\}$$

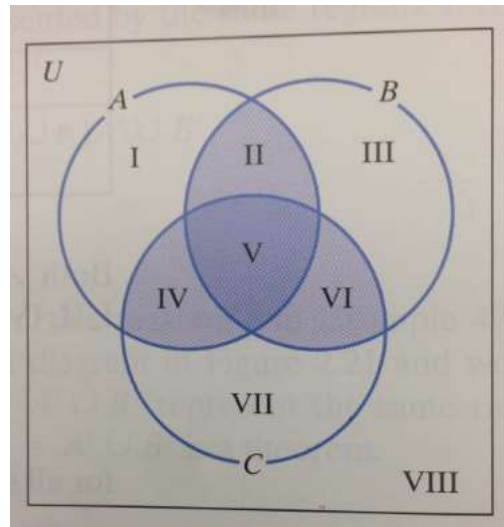
$$B = \{b, g, h\}$$

$$C = \{b, c, d, e, f\}$$

4. $A \cap (B \cup C)$
5. $C' \cap (A \cup B')$
6. $(B \cup C)' \cap A$

In Exercises 7-10, use the Venn diagram shown to answer each question

7. Which regions represent set C?
8. Which regions represent $B \cup C$?
9. Which regions represent $A \cap C$?
10. Which regions represent C' ?



In Exercises 11-16, use the Venn diagram to represent each set in roster form.

11. B

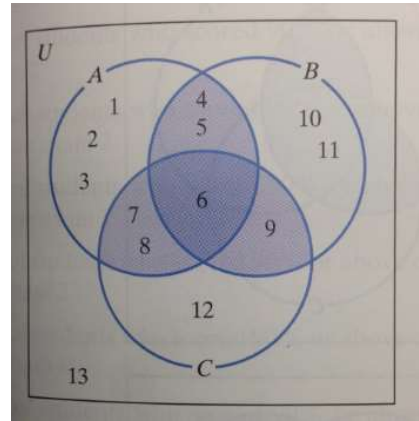
12. $B \cup C$

13. $(B \cup C)'$

14. $A \cap C$

15. $A \cup B \cup C$

16. $(A \cup B \cup C)'$

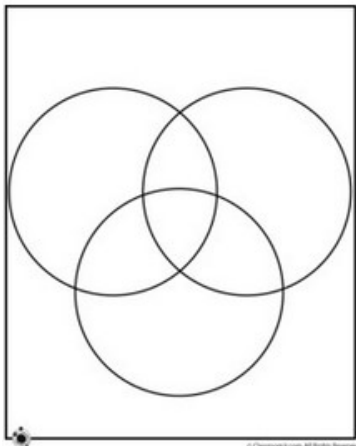


In Exercises 17-18 construct a Venn diagram illustrating the given sets

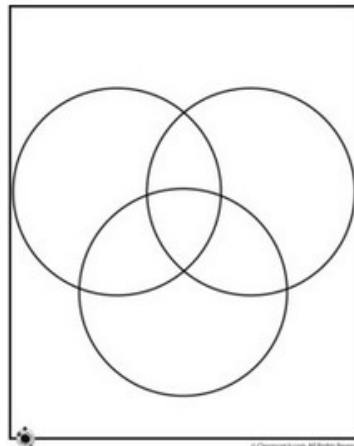
17. $A = \{a, e, h, i\}$, $B = \{b, c, e, f, h, i\}$, $C = \{e, f, g\}$, $U = \{a, b, c, d, e, f, g, h, i\}$

18. $U = \{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9\}$, $A = \{x_3, x_9\}$, $B = \{x_1, x_2, x_3, x_5, x_6\}$, $C = \{x_3, x_4, x_5, x_6, x_9\}$

17.



18.



Use the Venn diagram shown to solve Exercises 19-20. (and 21-23)

19. a. Which regions are represented by $A \cup B$?

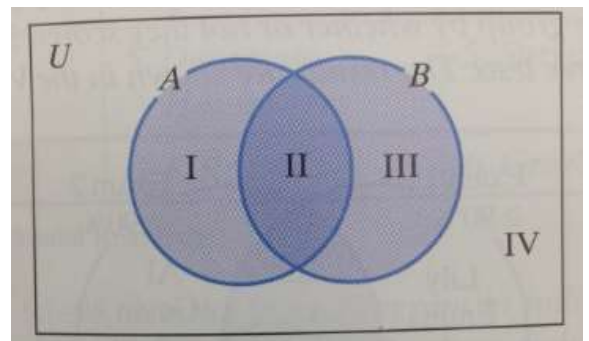
b. Which regions are represented by $B \cup A$?

c. Based on parts (a) and (b), what can you conclude?

20. a. Which region(s) is/are represented by $(A \cup B)'$?

b. Which region(s) is/are represented by $A' \cup B'$?

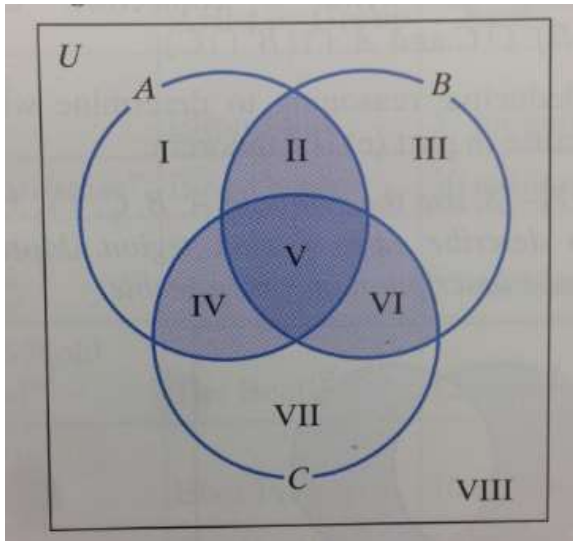
c. Based on parts (a) and (b), are $(A \cup B)'$ and $A' \cup B'$ equal for all sets A and B? Explain your answer.



In Exercises 21-23 Use the Venn diagram for 19-20 to determine whether the given sets are equal for all sets A and B.

21. $A' \cap B, A \cup B'$
22. $(A \cup B)', A' \cap B$
23. $(A \cup B')', A' \cap B$

Use the Venn diagram shown to solve Exercises 24-25. (and 26-28)



24.
 - a. Which regions are represented by $(A \cup B) \cap C$?
 - b. Which regions are represented by $(A \cap C) \cup (B \cap C)$?
 - c. Based on parts (a) and (b), what can you conclude?
25.
 - a. Which regions are represented by $C \cup (B \cap A)$?
 - b. Which regions are represented by $C \cap (B \cup A)$?
 - c. Based on parts (a) and (b), are $C \cup (B \cap A)$ and $C \cap (B \cup A)$ equal for all sets A, B, and C? Explain your answer.

In Exercises 26-28, use the Venn diagram shown above to determine which statements are true for all sets A, B, and C, and consequently, are theorems.

26. $A \cup (B \cap C) = (A \cup B) \cap C$
27. $B \cap (A \cup C) = (A \cap B) \cup (B \cap C)$
28. $A \cup (B \cap C)' = A \cup (B' \cup C')$